

Table of Laplace Transforms

In the following, all functions (signals) map \mathbf{R}_+ into \mathbf{R} .

General

Function	Laplace transform
$f(t)$	$F(s) = \int_0^\infty f(t)e^{-st} dt$
$f + g$	$F + G$
αf ($\alpha \in \mathbf{R}$)	αF
$\frac{df}{dt}$	$sF(s) - f(0)$
$\frac{d^k f}{dt^k}$	$s^k F(s) - s^{k-1} f(0) - s^{k-2} \frac{df}{dt}(0) - \dots - \frac{d^{k-1} f}{dt^{k-1}}(0)$
$g(t) = \int_0^t f(\tau) d\tau$	$G(s) = \frac{F(s)}{s}$
$f(\alpha t)$, $\alpha > 0$	$\frac{1}{\alpha} F(s/\alpha)$
$e^{at} f(t)$	$F(s - a)$
$t f(t)$	$-\frac{dF}{ds}$
$t^k f(t)$	$(-1)^k \frac{d^k F(s)}{ds^k}$
$\frac{f(t)}{t}$	$\int_s^\infty F(s) ds$
$g(t) = \begin{cases} 0 & 0 \leq t < T \\ f(t - T) & t \geq T \end{cases}$	$G(s) = e^{-sT} F(s)$

Specific

Function	Laplace transform
1	$\frac{1}{s}$
δ	1
$\delta^{(k)}$	s^k
t	$\frac{1}{s^2}$
$\frac{t^k}{k!}, k \geq 0$	$\frac{1}{s^{k+1}}$
e^{at}	$\frac{1}{s-a}$
$\cos \omega t$	$\frac{s}{s^2 + \omega^2} = \frac{1/2}{s - j\omega} + \frac{1/2}{s + j\omega}$
$\sin \omega t$	$\frac{\omega}{s^2 + \omega^2} = \frac{1/2j}{s - j\omega} - \frac{1/2j}{s + j\omega}$
$\cos(\omega t + \phi)$	$\frac{s \cos \phi - \omega \sin \phi}{s^2 + \omega^2}$
$e^{-at} \cos \omega t$	$\frac{s + a}{(s + a)^2 + \omega^2}$
$e^{-at} \sin \omega t$	$\frac{\omega}{(s + a)^2 + \omega^2}$